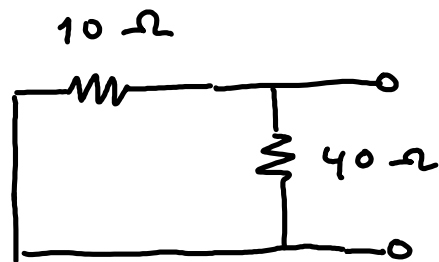
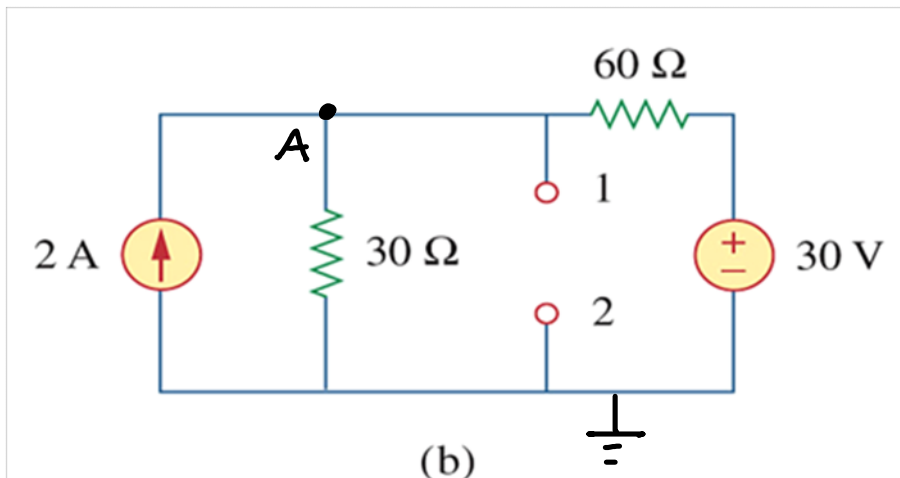


$$(a) \quad V_{Th} = \frac{4\Omega}{1\Omega + 4\Omega} \times 20 = \frac{4}{5} \times 20 = 16 \text{ V}$$

$$R_{Th} = 10 // 40 = \frac{10 \times 40}{10 + 40} = 8 \Omega$$



(b)



At node A

$$-2 + \frac{V_A}{30} + \frac{V_A - 30}{60} = 0$$

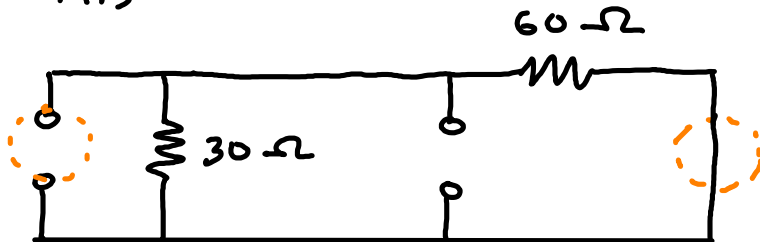
$$-120 + 2V_A + V_A - 30 = 0$$

$$3V_A = 150V$$

$$V_A = 50V$$

$$V_{TH} = V_A = \boxed{50V}$$

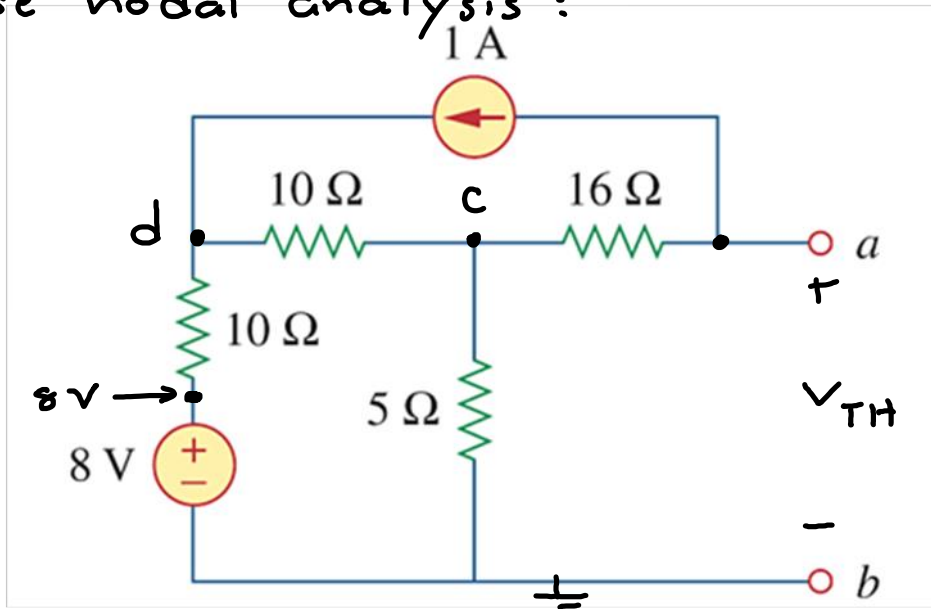
For R_{TH} , we deactivate all the sources:



$$R_{TH} = 30 // 60 = \frac{30 \times 60}{30 + 60} = \frac{10^2}{\cancel{30} \times \cancel{60}} = \boxed{20 \Omega}$$

First we find V_{TH}

Use nodal analysis:



KCL @ a:

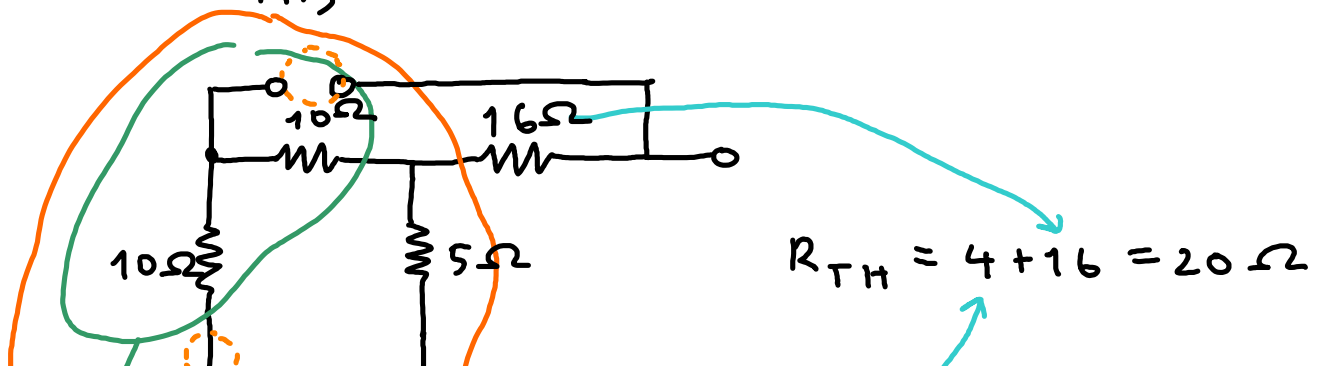
$$1 + \frac{V_a - V_c}{16} = 0$$

$$\frac{V_c - V_a}{16} = 1$$

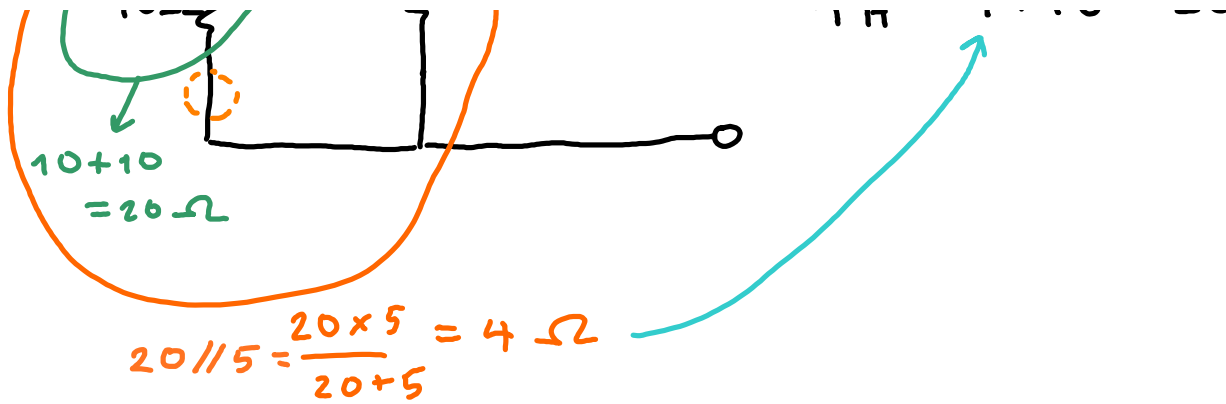
$$\left. \begin{aligned} \text{KCL @ c: } \frac{V_c - V_a}{16} + \frac{V_c - V_d}{10} + \frac{V_c}{5} &= 0 \\ \text{KCL @ d: } \frac{V_d - 8}{10} + \frac{V_d - V_c}{10} - 1 &= 0 \end{aligned} \right\} \Rightarrow \begin{aligned} V_c &= -\frac{2}{5} \\ V_d &= \frac{44}{5} \end{aligned}$$

$$V_a = V_c - 16 \times 1 = -\frac{2}{5} - 16 = -16.4 \text{ V} = V_{TH}$$

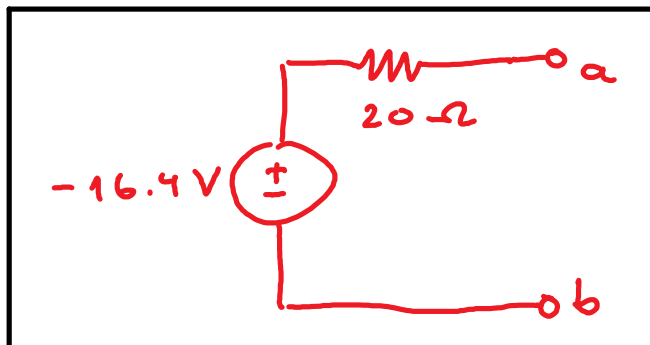
For R_{TH}, we deactivate all the sources:



$$R_{TH} = 4 + 16 = 20 \Omega$$

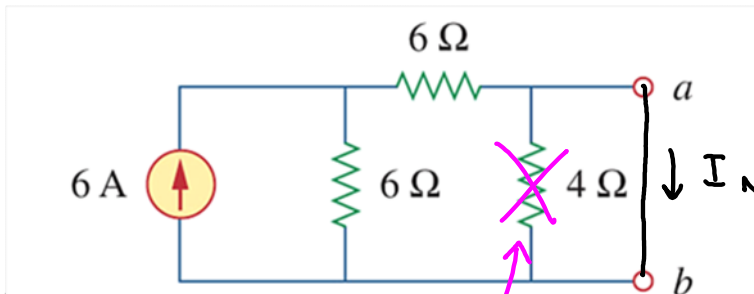


The Thevenin equivalent at terminal a-b is



First, we find I_N .

Recall that $I_N =$ short-circuit current



Alternatively, we see that the voltage across this 4Ω resistor is $V_a - V_b = 0$.

↑ same because they are shorted together.

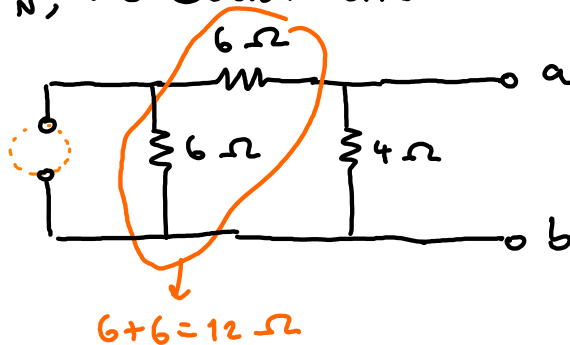
By ohm's law, there can't be any current through this 4Ω resistor.

The 4Ω resistor is gone because it is shorted out.

By the current divider formula, the $6A$ from the current source is split equally between the two 6Ω resistors.

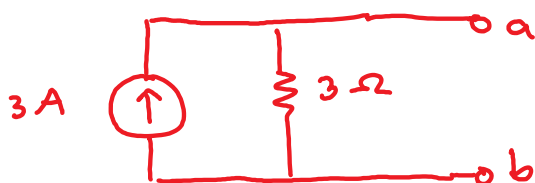
Hence, $I_N = 3A$.

For R_N , we deactivate all the sources:



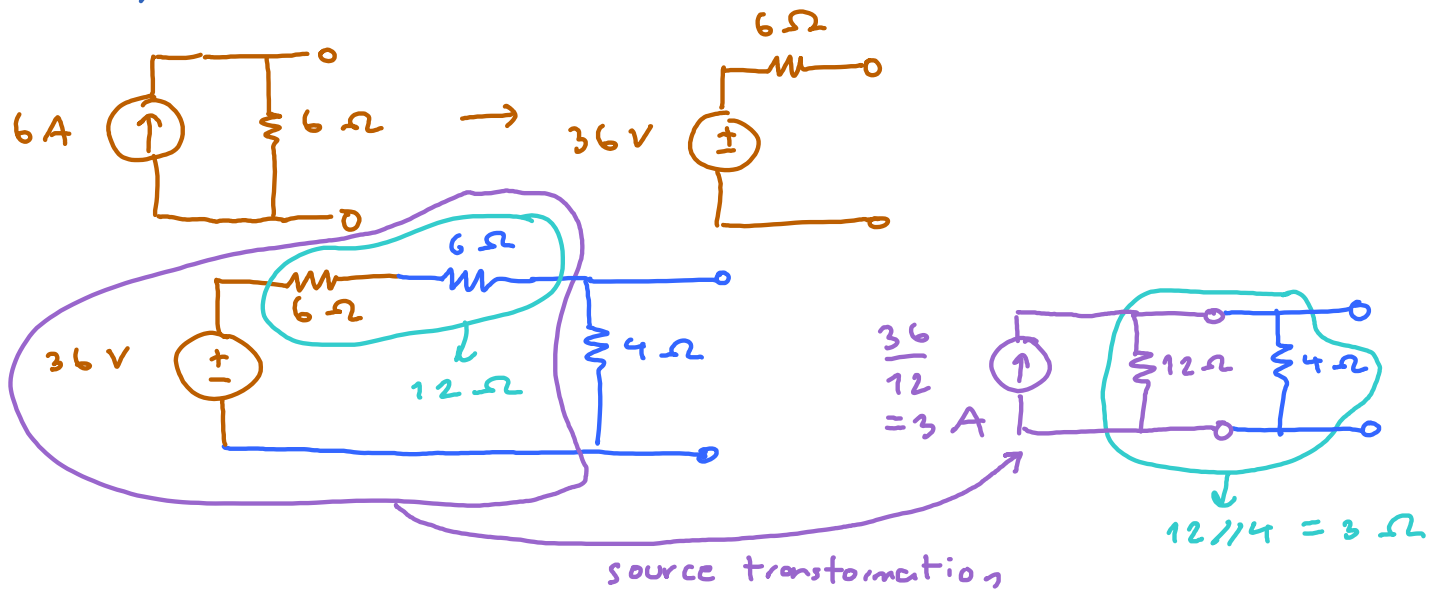
$$R_N = 12 // 4 = \frac{12 \times 4}{12 + 4} = 3 \Omega$$

The Norton equivalent is given by



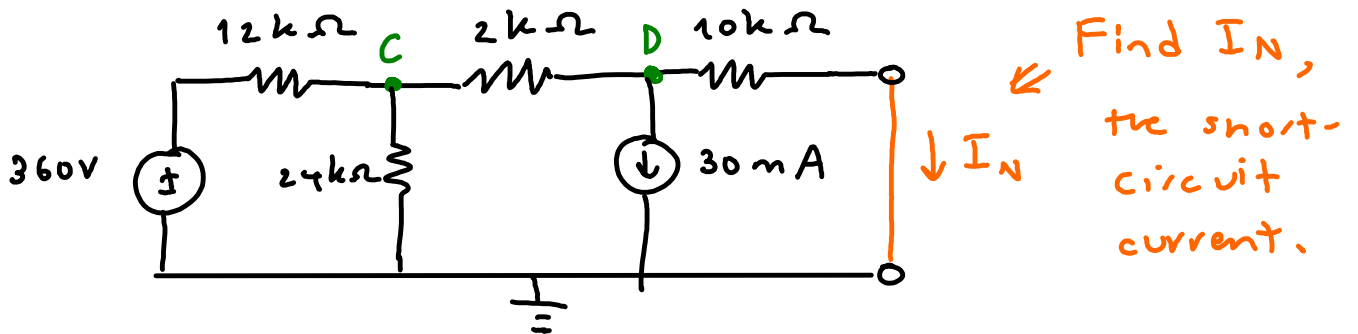
Alternatively, because the question does not specify that we

have to find the value of I_N and R_N from their definitions, we may choose to use source transformation:



which is the same as what we got from Norton's theorem above.

Note that the question specifies that we have to use the Norton theorem. Hence we will first need to find Norton equivalent of the following circuit



Find I_N , the short-circuit current.

Use Nodal analysis:

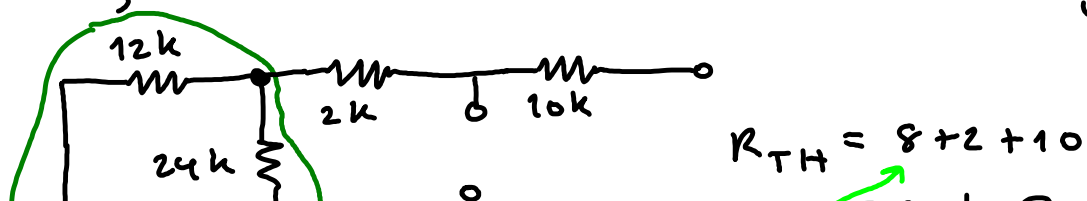
$$\left. \begin{aligned} \text{KCL @ } c \quad & \frac{V_c - 360}{12k} + \frac{V_c}{24k} + \frac{V_c - V_D}{2k} = 0 \\ \text{KCL @ } d \quad & 30m + \frac{V_D - V_c}{2k} + \frac{V_D}{10k} = 0 \end{aligned} \right\} \Rightarrow \begin{aligned} V_c &= 24V \\ V_D &= -30V \end{aligned}$$

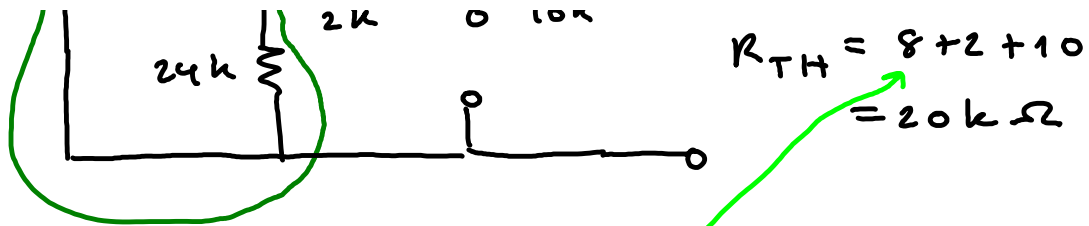
Note that

if I multiply these two equations by 1000, the m and k will magically disappear. So, I don't really have to care about them.

$$I_N = \frac{V_D}{10k} = \frac{-30}{10k} = -3mA$$

For R_N , we deactivate all the source and get

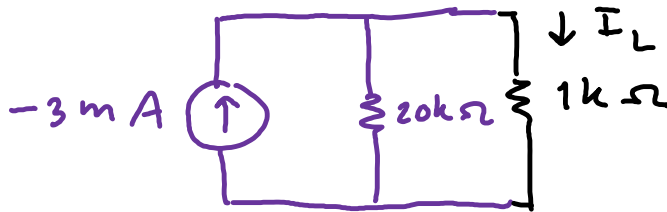




$$12k // 24k$$

$$= \frac{12 \times 24}{12 + 24} k = 8k$$

Now, we connect the Norton equivalent back to the load resistor:



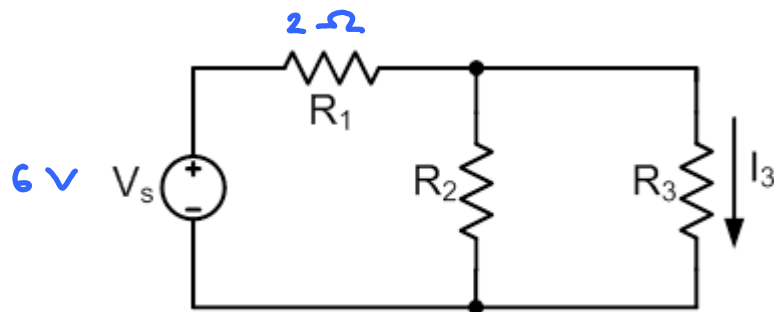
The current I_L is = $-3m \times \frac{1k}{\frac{1k}{1k} + \frac{1}{20k}}$ = $-3 \times \frac{20}{21} mA$

↑
current divider

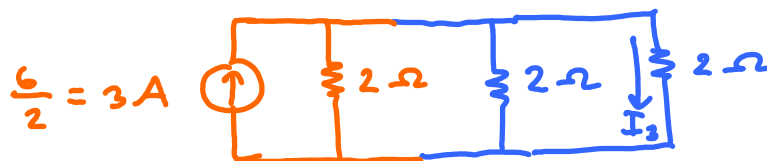
$$V_o = I_L \times R_L = -3 \times \frac{20}{21} \times 1k = \boxed{-\frac{60}{21} V \approx -2.86 V}$$

[ECS203, Midterm Exam, 2009-2, Q1]

Monday, July 08, 2013 7:40 PM



(a) we transform V_s and R_1



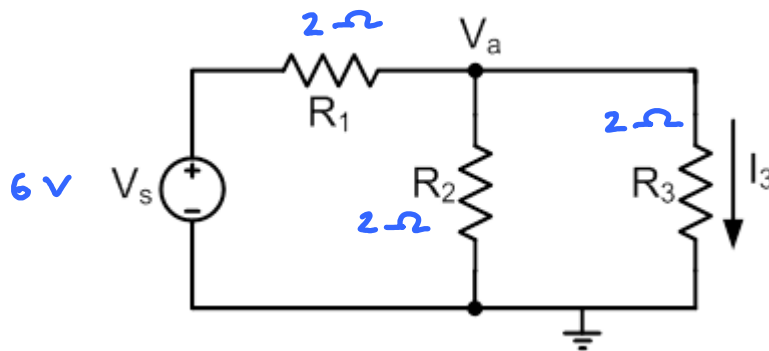
current divider

$$I_3 = \frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{2} + \frac{1}{2}} \times 3 \text{ A}$$

$$= \frac{1}{3} \times 3 \text{ A}$$

$$= \boxed{1 \text{ A}}$$

(b)



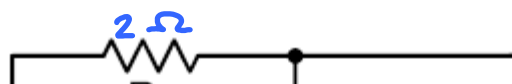
$$\frac{V_a - 6}{2} + \frac{V_a}{2} + \frac{V_a}{2} = 0$$

$$3V_a - 6 = 0$$

$$V_a = \frac{6}{3} = 2 \text{ V}$$

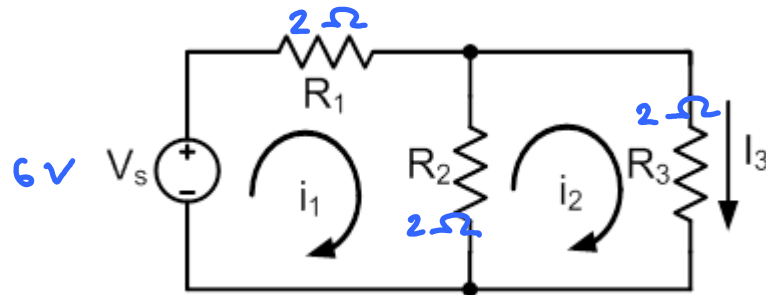
$$I_3 = \frac{V_a}{R_3} = \frac{2}{2} = \boxed{1 \text{ A}}$$

(c)



... that

(c)



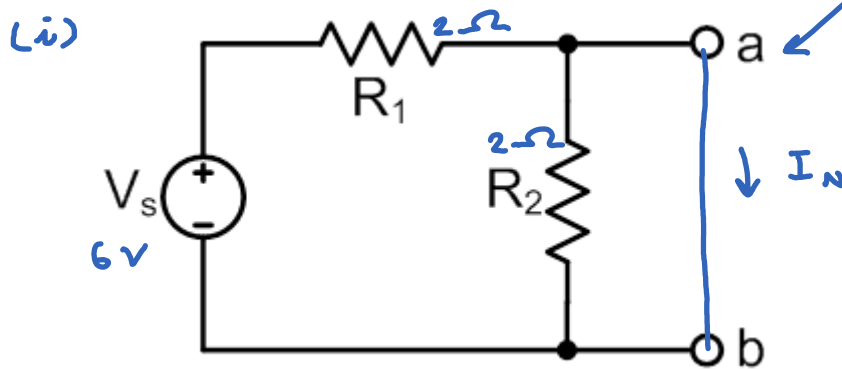
Note that $I_3 = i_2$.

$$\left. \begin{aligned} 6 - i_1 \times 2 - (i_1 - i_2) \times 2 &= 0 \\ -(i_2 - i_1) \times 2 - i_2 \times 2 &= 0 \end{aligned} \right\} \Rightarrow$$

$$\begin{aligned} i_1 &= 2A \\ i_2 &= 1A \\ I_3 &= 1A \end{aligned}$$

$$\begin{aligned} 2i_1 - i_2 &= 3 \\ i_1 - 2i_2 &= 0 \\ i_1 &= 2i_2 \\ 4i_2 - i_2 &= 3 \\ 3i_2 &= 3 \\ i_2 &= \frac{3}{3} = 1A \\ i_1 &= 2 \times i_2 \\ i_1 &= 2A \end{aligned}$$

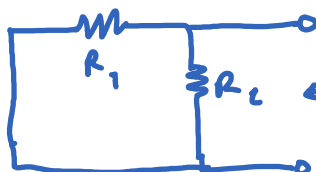
(d)



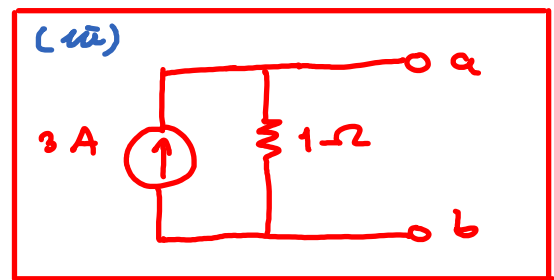
To find I_N , we add this short-circuit connection.

$$I_N = \frac{V_s}{R_1} = \frac{6}{2} = 3A$$

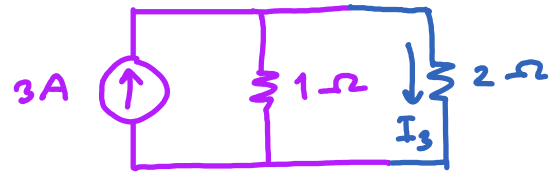
(ii) To find R_N , we deactivate the source.



$$R_N = R_1 // R_2 = 2 // 2 = 1 \Omega$$



(c)



$$I_3 = \frac{\frac{1}{2}}{\frac{1}{1} + \frac{1}{2}} \times 3$$
$$= \frac{1}{3} \times 3 = \boxed{1\text{A}}$$